On solid solutions in the system LiF-Na₃AlF₆*

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The quasi-binary system $\text{LiF}-\text{Na}_3\text{AlF}_6$ has been studied using the methods of TA and X-ray phase analysis. It has been found that there is a eutectic point (85.0 ± 1) mole % LiF, (15.0 ± 1) mole % Na₃AlF₆, $T_{\rm E} = (696 \pm 1)$ °C in the system. On the side of Na₃AlF₆ there is a narrow region of limited solid solutions containing up to 6 mole % LiF, 94 mole % Na₃AlF₆ at the eutectic temperature. The results of TA and X-ray phase analysis are consistent with the conclusions which follow from the thermodynamic analysis of the course of liquidus curve of Na₃AlF₆ in the vicinity of the temperature of fusion of pure cryolite in the studied system.

Lithium fluoride appears to be one of the most promising additions to the electrolytes for aluminium production [1, 2]. Therefore it is topical to investigate the interaction between LiF and the usually used constituents of these electrolytes, particularly Na_3AlF_6 .

The system $\text{LiF}-\text{Na}_3\text{AlF}_6$ may be considered as a quasi-binary section of the ternary reciprocal system $\text{Li},\text{Na} \parallel \text{F},\text{AlF}_6$. This system has been studied six times [3-8]up to now. However, there are great differences among the published results (Table 1). *Chu* and *Belyaev* [3] have investigated only the course of the liquidus curve in the system and the coordinates of the eutectic point by the visual-polythermic analysis. *Holm* [4] and later *Jenssen* [5] have determined also the character of the system. According to these authors the system is a simple eutectic one. They investigated the system by TA and DTA methods. *Kuvakin* [6] used the TA method and he found that the system is eutectic with a broad region of solid solutions of LiF in Na₃AlF₆. However, comparing his results with those of the other authors, the temperature of the eutectic crystallization seems to be very low. *Matiašovský* and *Malinovský* [7] found on the basis of TA and X-ray phase analysis also an extensive solid solution on the side of Na₃AlF₆. *Holm* [8] in his other work has found a not too broad region of solid solutions of LiF in Na₃AlF₆. Because of serious discrepancies in published results it has been decided to examine once more the discussed system.

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Table 1

М.р. [°С]		$T_{\rm E}$	Eutectic composi- tion [mole %]		Type of	Remarks (extent of solid	Ref.
Na ₃ AlF ₆	LiF	[°C]	LiF	Na ₃ AlF ₆	diagram	solution of LiF in Na ₃ AlF ₆)	
1002	845	700	83.5	16.5	_	Liquidus only	[3]
1011	848	693			SES		[4]
1011	848	693	84.6	15.4	SES	_	[5]
1000	848	665	75	25	\mathbf{ES}	43 mole %	[6]
1004	847	700	85.6	14.4	ES	70 mole %	[7]
1010	848	694	85	15	\mathbf{ES}	12 mole %	[8]
1008	848	696	85	15	ES	6 mole %	This worl

The main parameters of $LiF - Na_3AlF_6$ system according to different authors

SES — simple eutectic system; ES — eutectic system.

One of the most interesting is the question of the existence of limited solid solutions in the studied system. The existence of limited solid solutions in the system LiF-NaFwhich can be considered to some extent as an analogue of the $\text{LiF}-\text{Na}_3\text{AlF}_6$ system favours the idea of the existence of the limited solid solutions in the system under study. In the LiF-NaF system there are limited solid solutions on the side of NaF up to (4 ± 1) mole % LiF, (96 ± 1) mole % NaF at the temperature of the eutectic crystallization [9, 10]. Therefore the problem of the existence of the solid solution in the system LiF-- $-\text{Na}_3\text{AlF}_6$ has been studied carefully in this work.

The oretical

It can be proved [11] that if there is a limited solid solution on the base of component B in the system A-B (see Fig. 1) then it holds

$$\ln \frac{a_{\rm B}^{\rm l}}{a_{\rm B}^{\rm s}} = \frac{\Delta H_{\rm B}^{\rm f}}{R} \left[\frac{1}{T_{\rm B}^{\rm f}} - \frac{1}{T_{\rm B}} \right],\tag{1}$$

where $a_{\rm B}^{\rm l}$ is the activity of component B in liquid solution, which is saturated at $T_{\rm B}^{\rm s}$ with solid solution of B in A (point "1" in Fig. 1), $a_{\rm B}^{\rm s}$ is the activity of component B in the solid solution A + B at the temperature $T_{\rm B}$ (point "2" in Fig. 1), $\Delta H_{\rm B}^{\rm f}$ is the enthalpy of fusion of pure component B, $T_{\rm B}^{\rm f}$ is the temperature of fusion of pure component B, $T_{\rm B}$ is the temperature of primary crystallization of the solid solution A + B, the composition of which corresponds to the point "2" (Fig. 1).

Relation (1) was derived on the assumption that $\Delta C_P^{l/s}$ of component B equals zero. Because we shall analyze the course of the liquidus and solidus curves near the point T_B^f the mistake caused by this simplification is negligible.

It follows from eqn (1) that the ratio a^{1}/a^{s} is only a function of the parameters, which are characteristic of pure substance B (and of course of temperature).

If the difference $1 - x_{\rm B}^{\rm l}$ is small $(x_{\rm B}^{\rm l}$ being the mole fraction of component B in the liquid phase of the system A-B which is at $T_{\rm B}$ in equilibrium with the limited solid

(2)

solution on the basis of substance B), the function $a_{\rm B}^{\rm l} = f(x_{\rm B}^{\rm l})$ can be expressed with sufficient accuracy by means of the universal relationship [12]:

 $a_{\mathrm{B}}^{\mathrm{l}} = (x_{\mathrm{P}}^{\mathrm{l}})k^{\mathrm{St}}_{\mathrm{A/B}}.$

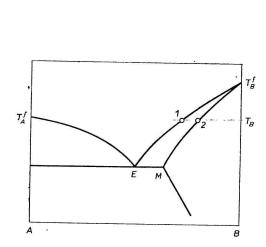


Fig. 1. Scheme of the phase diagram of a binary system A-B having limited solid solution on the base of component B.

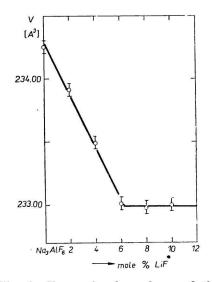


Fig. 2. Change in the volume of the unit cell of Na_3AlF_6 owing to the formation of the solid solution of LiF in Na_3AlF_6 .

where $k_{A/B}^{\text{St}}$ is the Stortonbeker correction factor [13, 14]. It is equal to the number of new particles which appear in the system formed by pure liquid substance B when I molecule of substance A is added.

An analogous equation can be applied in order to express the functional dependence $\alpha_{\rm B}^{\rm s} = f(x_{\rm B}^{\rm s})$. Here $x_{\rm B}^{\rm s}$ is the mole fraction of component B in the limited solid solution saturated at $T_{\rm B}$ with substance B. The Stortenbeker correction factor has in this case an analogous meaning as it has been explained above. Thus

$$a_{\rm B}^{\rm s} = (x_{\rm B}^{\rm s})k^{\rm St}k^{\rm A/B}.$$
(3)

Inserting from eqns (2) and (3) into eqn (1) we obtain

$$k_{A/B}^{\rm St} \ln x_{\rm B}^{\rm l} = \Delta H_{\rm B}^{\rm f} (1/T_{\rm B}^{\rm f} - 1/T_{\rm B})/R + k_{A/B}^{\rm St} \ln x_{\rm B}^{\rm s}.$$
 (4)

Because $x_{\rm B}^{\rm s} < 1$ one can write formally

$$k_{\rm A/B}^{\rm St} \ln x_{\rm B}^{\rm s} = \Delta H_{\rm B}^{\rm s} (1/T_{\rm B}^{\rm f} - 1/T_{\rm B})/R.$$
 (5)

The quantity $\Delta H_{\rm B}^{\rm s} > 0$ has the same physical dimensions as $\Delta H_{\rm B}^{\rm f}$. Inserting from eqn (5) into eqn (4) and rearranging we get

$$k_{\text{A/B}}^{\text{St}} \ln x_{\text{B}}^{\text{l}} = (\Delta H_{\text{B}}^{\text{f}} + \Delta H_{\text{B}}^{\text{s}}) (1/T_{\text{B}}^{\text{f}} - 1/T_{\text{B}})/R$$

or

Evidently

$$k_{A/B}^{\text{St}} \ln x_{B}^{\text{l}} = \Delta H_{B}^{\bullet}(1/T_{B}^{\text{f}} - 1/T_{B})/R.$$
(6)

$$\Delta H^{\bullet}_{\rm B} = \Delta H^{\rm f}_{\rm B} + \Delta H^{\rm s}_{\rm B}.$$

The cryometric treatment of the data concerning the course of the liquidus curve of B enables us to determine the value of the slope of the tangent to the liquidus curve at the melting point of pure component B. This quantity will be denoted as $k_{\rm B}^{0,1}$. It follows from eqn (6) that

$$k_{\rm B}^{0,1} = \lim_{x_{\rm B} \to 1} ({\rm d}T/{\rm d}x_{\rm B}) = R(T_{\rm B}^{\rm f})^2 \, k_{\rm A/B}^{\rm St} / \mathcal{A}H_{\rm B}^{\bullet}.$$
 (7)

In the case of the system $\text{LiF}-\text{Na}_3\text{AlF}_6$, the first component yields Li^+ and F^- ions, the second one the ions Na^+ , AlF_6^3 -, F^- and most probably also AlF_4^- [15]. Thus if A = = LiF, $B = \text{Na}_3\text{AlF}_6$, then $k_{A/B}^{\text{St}} = 1$ (*i.e.*, Li⁺). If $A = \text{Na}_3\text{AlF}_6$, B = LiF, then $k_{A/B}^{\text{St}} =$ = 4 (*i.e.*, three ions Na^+ and one ion Al^{3+} , probably in the form of complex anions AlF_6^3 - and AlF_4^-).

Because $\Delta H_{\rm B}^{\rm f} < \Delta H_{\rm B}^{\rm h}$, the slope $k_{\rm B}^{0,l}$ is smaller if there exist limited solid solutions than if there are no solid solutions in the system at all. Consequently if the difference $\Delta H_{\rm B}^{\rm h} - \Delta H_{\rm B}^{\rm f}$ where $\Delta H_{\rm B}^{\rm f}$ is the enthalpy of fusion of pure B determined *e.g.* from calorimetric measurements is greater than the admissible experimental error it follows that there is a region of solid solutions near the point $T_{\rm B}^{\rm f}$. Therefore a careful cryometric treatment of the course of the liquidus curve near the melting point of a given component indicates the existence of limited solid solutions based on the given component.

Experimental

LiF of grade "for single crystals", m.p. 848°C was used. Cryolite was prepared from NaF of grade "for single crystals", m.p. 992°C and from AlF₃ prepared by sublimation of pure salt in a platinum apparatus [16]. Temperature was measured by means of Pt//Pt10Rh thermocouple calibrated by means of melting points of pure K₂SO₄ (1069°C), NaF (992°C), Na₂SO₄ (884.8°C), NaCl (800.8°C), KCl (772°C), and eutectic mixture 81 mole % KCl + 19 mole % LiF (718°C). The mixtures of salts (20 g weighed-in) were melted in a platinum crucible with a minimal over-heating. The signal of thermocouple was registered by a compensating recorder EZ 11. The cooling rate was 1-3°C/min. Twenty-nine inner mixtures of the LiF—Na₃AlF₆ system have been investigated. The results which are important from the point of view of the existence of limited solid solutions are presented in Table 2.

The samples for X-ray phase analysis were prepared in the following way: 10 g of salt mixture was melted in a Pt crucible with minimal over-heating above the melting temperature and after thorough stirring the mixture was cooled with the rate $1-2^{\circ}$ C/min to 690°C, *i.e.* slightly below the temperature of the eutectic crystallization. The sample was kept for 30 min at this temperature. Then the crucible was cooled in crushed ice which proved to be a better cooling medium than solid CO₂. Then the solidified sample was crushed and studied by X-ray analysis.

The samples contained 0, 2, 4, 6, 8, and 10 mole % LiF, rest Na₃AlF₆.

A Phillips diffractometer (goniometer PW 1050 and generator PW 1130) was used for the measurements. The X-ray radiation was obtained from a Cu anode tube with a Ni filter at 45 kV and 20 mA. The divergence and scatter slits were 1° and the receiving slit 0.1 mm. The time constant of the recorder T = 4, goniometer speed 1/4° 20/min, chart speed 1200 mm/hr. Silicon was used as the inner standard for the measurements of lattice parameters. The refinement of the lattice parameters of Na₃AlF₆ was done on the basis of twelve diffraction lines from the region of angles $46-35^{\circ}$ 20. Five diffraction records were done for each sample. The refinement of the lattice parameters was done using the least square method according to *Lindquist*'s program [17].

Table 2

T 'T		Temperature [°C]		
LiF [mole %]	Na ₃ AlF ₆ - [mole %]	Primary crystallization	Eutectic crystallization	
100		848		
99.75	0.25	843	690	
99.50	0.50	840	694	
99.25	0.75	836	695	
99.0	1.0	833	696	
98.0	2.0	819	696	
97.0	3.0	807	696	
96.0	4.0	795	696	
95.0	5.0	785	697	
86.0	14.0	703	696	
85.0	15.0		696	
10.0	90.0	999	2000 - 100 -	
7.5	92.5	1000	—	
5.0	95.0	1003		
4.0	96.0	1004	-	
2.0	98.0	1005.5		
1.0	99.0	1007		
	100	1008		

TA data concerning the system LiF-Na₃AlF₆

The existence of limited solid solutions has been proved also by the X-ray analysis. It has been found that the volume of the elementary cell of pure Na₃AlF₆ equals 234.25 \pm \pm 0.1 A³. The volume of the elementary cell of the solid solution containing 94 mole % Na₃AlF₆ + 6 mole % LiF is 233.00 \pm 0.1 A³. The decrease is fluent and the volume of the elementary cell remains constant despite a further increase in concentration of LiF (Fig. 2).

Discussion

A. Region with high concentration of LiF

From the results of TA it follows that there are no solid solutions on the side of LiF. The eutectic halt has been found on the cooling curve even at the concentration 99.75 mole % LiF, 0.25 mole % Na₃AlF₆.

By the cryometric treatment of the experimental results of TA it was found that ΔH^* (LiF) = 6243 cal mol⁻¹, which differs from the calorimetric value of ΔH^t reported by *Douglas* and *Dever* [18] *i.e.* 6471 cal mol⁻¹ by 3.5%, this being in the limits of experimental error.

B. Region with high concentration of Na₃AlF₆

From the results of TA it follows that the eutectic halt cannot be found on the cooling curves if the mixtures contain more then 90 mole $\% Na_3AlF_6$.

By the cryometric treatment of the results of TA for the liquidus curve of Na₃AlF₆ it has been found that ΔH^* (Na₃AlF₆) = 35 500 cal mol⁻¹, which differs from the calorimetric value $\Delta H^{\rm f} = 25$ 640 cal mol⁻¹ [19] by 38.4%. Even if the value of $\Delta H^{\rm f}$ (Na₃AlF₆) = = 27 600 cal mol⁻¹ reported by *Kelley* [20] was used, ΔH^* (Na₃AlF₆) would be by 28.6% greater. The difference $\Delta H^* - \Delta H^{\rm f}$ exceeds in this case about three times the possible experimental error.

Thus from the cryoscopic measurements it follows that the solid solutions based on Na_3AlF_6 do exist.

In this connection the results of X-ray phase analysis are conclusive. From Fig. 2 it follows that the volume of the unit cell of Na_3AlF_6 changes as the solid solution of LiF in Na_3AlF_6 is formed. This result confirms again the existence of limited solid solutions of LiF in Na_3AlF_6 . At the eutectic temperature the range of the solid solutions is up to 6 mole % LiF, 94 mole % Na_3AlF_6 . This result is in agreement with the results of TA as well as with the cryometric data.

Consequently it may be stated that the system $\text{LiF}-\text{Na}_3\text{AlF}_6$ is quasi-binary with the eutectic point having coordinates 85.0 mole % LiF, 15.0 mole % Na}3AlF_6 and temperature $T_{\text{E}} = 696^{\circ}\text{C}$.

On the side of Na₃AlF₆ there is a limited solid solution with limit concentration at $T_{\rm E}$ equal to 6 mole % LiF, 94 mole % Na₃AlF₆ according to X-ray data. The TA data seem to indicate a some broader extent of solid solution, approx. up to 10 mole % LiF, 90 mole % Na₃AlF₆.

The results reported in this paper are thus in very good agreement with the data by Holm [8] concerning the coordinates of the eutectic point E in the system LiF – Na₃AlF₆ and in an acceptable agreement concerning the extent of limited solid solution of LiF in Na₃AlF₆.

The previous data by Holm [4] as well as by Jenssen [5] who have claimed the simple eutectic character of the LiF-Na₃AlF₆ system have not been confirmed.

The data by Kuvakin [6] concerning both the composition and temperature of the eutectic point and the extent of solid solution seem to be erroneous.

The data reported by *Matiašovský* and *Malinovský* [7] on the extent of solid solution of LiF in Na₃AlF₆ are evidently too high.

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